

Day 4 Notes:

changed!

Solve each trigonometric equation. All trig answers are $0 \leq \theta < 2\pi$ and may need a calculator.

Ex: $2\sin(\theta) + 1 = 0$

$\sin \theta = -1/2$
 $\theta = 7\pi/6, \theta = 11\pi/6$

Ex: $3\tan^2(\theta) - 1 = 0$

$\tan^2 \theta = 1/3$
 $\tan \theta = \pm \sqrt{3}/3$
 $\theta = \pi/6, 5\pi/6, 7\pi/6, 11\pi/6$

Ex: $\csc^2(\theta) = 2$

$\sin^2 \theta = 1/2$
 $\theta = \pi/4, 3\pi/4, 5\pi/4, 7\pi/4$

Ex: $\sin^2(\theta)\cos(\theta) = 4\cos(\theta)$

$\cos \theta (\sin \theta - 2)(\sin \theta + 2) = 0$
 $\cos \theta = 0$
 $\pi/2, 3\pi/2$

Ex: $\cos^2(\theta) - 4\cos(\theta) + 3 = 0$

$(\cos \theta - 3)(\cos \theta - 1) = 0$
 $\cos \theta = 1$
 $\theta = 2\pi, 0$

Ex: $1 - \cos(\theta) = \sqrt{3}$

$\cos \theta = -\sqrt{3} + 1$
 $\theta = \arccos(-\sqrt{3} + 1)$

Ex: $\sin(\theta) = \sin(-\theta) + 1$

$\sin \theta = -\sin \theta + 1$
 $2\sin \theta - 1 = 0$
 $\theta = \pi/6, 5\pi/6$

Ex: $\tan^2(\theta) = \sin(\theta)\sec(\theta)$

$\tan^2 \theta = \tan \theta$
 $\tan^2 \theta - \tan \theta = 0$
 $\tan \theta = 0, \tan \theta - 1 = 0$
 $\theta = 2\pi, 0, \theta = \pi/4, 5\pi/4$

Ex: $3\cos(\theta) - 5 = 0$

$\cos \theta = 5/3$
 $\theta = \text{DNE}$

Ex: $\csc^2(\theta) - 2\cot(\theta) = 0$

$1 + \cot^2 \theta - 2\cot \theta = 0$
 $(\cot \theta - 1)(\cot \theta - 1) = 0$
 $\cot \theta = 1$
 $\theta = \pi/4, 5\pi/4$

Ex: $\sec^2(\theta) + \sec(\theta) - 2 = 0$

$(\sec \theta + 2)(\sec \theta - 1) = 0$
 $\sec \theta = -2, \sec \theta = 1$
 $\theta = 2\pi/3, 4\pi/3, \theta = 2\pi, 0$

Ex: $\tan(\theta) - \sec(\theta) = \sqrt{3}$

$\tan \theta = \sec \theta + \sqrt{3}$
 $\tan^2 \theta = \sec^2 \theta + 2\sqrt{3}\sec \theta + 3$
 $\sec^2 \theta - 1 = \sec^2 \theta + 2\sqrt{3}\sec \theta + 3$
 $0 = 2\sqrt{3}\sec \theta + 4$
 $-2\sqrt{3}/3 = \sec \theta$
 $\theta = \arccos(-2\sqrt{3}/3)$
 ~~$\theta = \pi/6, 7\pi/6$~~ extraneous

Ex: $(\cot(\theta) - \sqrt{3})^2 = \csc^2(\theta)$

$\cot^2 \theta - 2\sqrt{3}\cot \theta + 3 = 1 + \cot^2 \theta$
 $-2\sqrt{3}\cot \theta + 2 = 0$
 $\cot \theta = 1/\sqrt{3}$ or $3/\sqrt{3}$
 ~~$\theta = \pi/3$~~ $\theta = 4\pi/3$

Ex: $4\cos^2(\theta) - 5\cos(\theta) + 1 = 0$

$(4\cos \theta - 1)(\cos \theta - 1) = 0$
 $\cos \theta = 1/4, \cos \theta = 1$
 $\theta = \arccos(1/4), \theta = 2\pi, 0$
 $\theta = 2\pi - \arccos(1/4)$

Ex: $\sqrt{2}\csc^2(\theta) + \csc(\theta) = \sqrt{2}$ extraneous

$(\sqrt{2}\csc \theta - 1)(\csc \theta + \sqrt{2}) = 0$
 $\csc \theta = 1/\sqrt{2}, \csc \theta = -\sqrt{2}$
 DNE. $\theta = 5\pi/4, 7\pi/4$

Ex: $2\tan^2(\theta) - 3\sec(\theta) + 3 = 0$

$2(\sec^2 \theta - 1) - 3\sec \theta + 3 = 0$
 $(2\sec \theta - 1)(\sec \theta - 1) = 0$
 $\sec \theta = 1/2, \sec \theta = 1$
 DNE $\theta = 2\pi, 0$